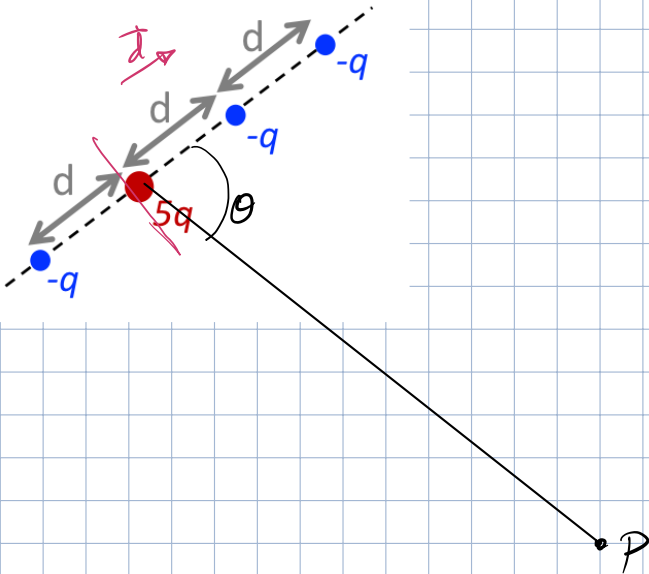


$$\begin{aligned}\vec{A} &= \frac{\mu_0}{4\pi} \int \frac{J(\vec{r}')}{R} d\tau' = \frac{\mu_0}{4\pi} \int \frac{I d\vec{r}'}{|\vec{r} - \vec{r}'|} = \frac{\mu_0}{4\pi} \frac{1}{r^{2.5}} \int P_1(\cos\theta) (r')^2 dl' \\ &= \frac{\mu_0}{4\pi} \left[\cancel{\frac{1}{r}} \int dl' + \frac{1}{r^2} \int r' \cos\theta dl' + \dots \right] \\ &= \frac{\mu_0}{4\pi} \frac{1}{r^2} \cdot \int (\vec{r}' \cdot \hat{r}) dl\end{aligned}$$

kl an Midterm 2



$$Q_{\text{tot}} = 2q \neq 0$$

$$V_{\text{mono}} = \frac{1}{4\pi\epsilon_0} \frac{Q_{\text{tot}}}{r^2}$$

dependent on coordinate system

$$\begin{aligned}\vec{p} &= \int \vec{r}' \rho(\vec{r}') d\tau' = \sum \vec{r}'_i q_i \\ &= -q(-d) + 5q(0) + (-q)(d) + (-2q)(2d) \\ &= d(+q - q - 2q) = -2qd\end{aligned}$$

$$V_{\text{dip}} = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{-2qd \cos\theta}{r^2} \hat{r}$$

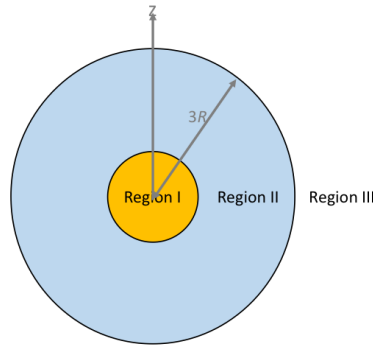
$$\begin{aligned}V_{\text{quad}} &= \frac{1}{4\pi\epsilon_0} \left[\frac{1}{r^3} \int r'^2 \left(\frac{3}{2} \cos^2\theta - \frac{1}{2} \right) d\tau' \right] \\ &= \frac{1}{4\pi\epsilon_0} \frac{1}{r^3} \sum_i (r'_i)^2 \cdot q_i \left(\frac{3}{2} \cos^2\theta - \frac{1}{2} \right)\end{aligned}$$

Consider a sphere of radius $3R$ and three Regions:

- Region I = a concentric sphere with radius R
- Region III = outside of the sphere with radius $3R$
- Region II = between Region I and Region III

Assume that

- electric potential in Region I is $V(I) = C_1$
- electric potential in Region III is $V(III) = C_3 \frac{3R}{r} \cos\theta$



where C_1 and C_3 are constant, r is radial distance from the center of the spheres and θ is the polar angle from the z direction.

Calculate the electric potential in Region II, using the "separation of variables" method.

Hint: You can solve this problem by writing down potentials in the three regions and applying two boundary conditions: one at $r=R$ and the other at $r=3R$.

$$V_I = C_1 \cdot P_0 + 0 \cdot P_1 + 0 \cdot P_2 + \dots$$

$$V_{II} = \sum_l \left(A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos\theta)$$

$$V_{III} = C_3 \frac{3R}{r} \cos\theta = C_3 \frac{3R}{r} P_1$$

	<u>$l=0$</u>	<u>$l=1$</u>	<u>$l>1$</u>
V_I	C_1	0	0
V_{II}	$(A_0 + \frac{B_0}{r}) P_0$	$(A_1 r + \frac{B_1}{r^2}) P_1$	$(A_l r^l + \frac{B_l}{r^{l+1}}) P_l$
V_{III}	0	$C_3 \frac{3R}{r} P_1$	0

$$\text{at } r=R \quad A_0 + \frac{B_0}{R} = C_1$$

$$\text{at } r=3R \quad A_0 + \frac{B_0}{3R} = 0$$